

**Midterm Test**

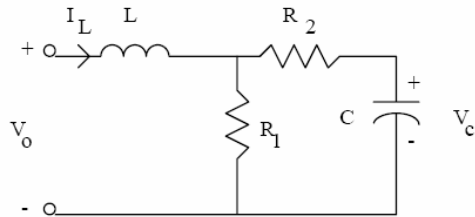
Name \_\_\_\_\_  
 Print \_\_\_\_\_

1. Solve the initial value problem using the Laplace transform (5 pts)

$$\frac{d^2 y}{dt^2} + 5 \frac{dy}{dt} + 4y = e^{-2t}, \quad y(0) = 0, \quad y'(0) = 1.$$

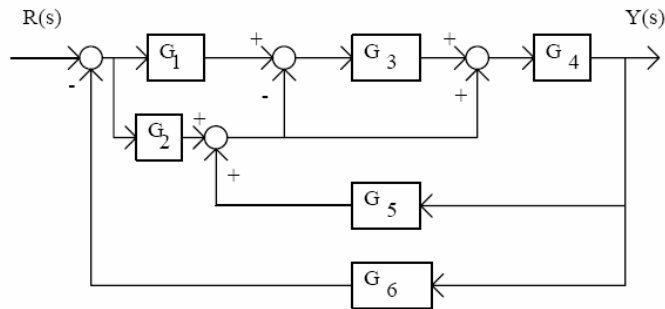
Find such that  $y'' - y' + y = u$  that the poles of system will be  $-2$  and  $-3$ . (5 pts)

2. Given the network (6 pts)

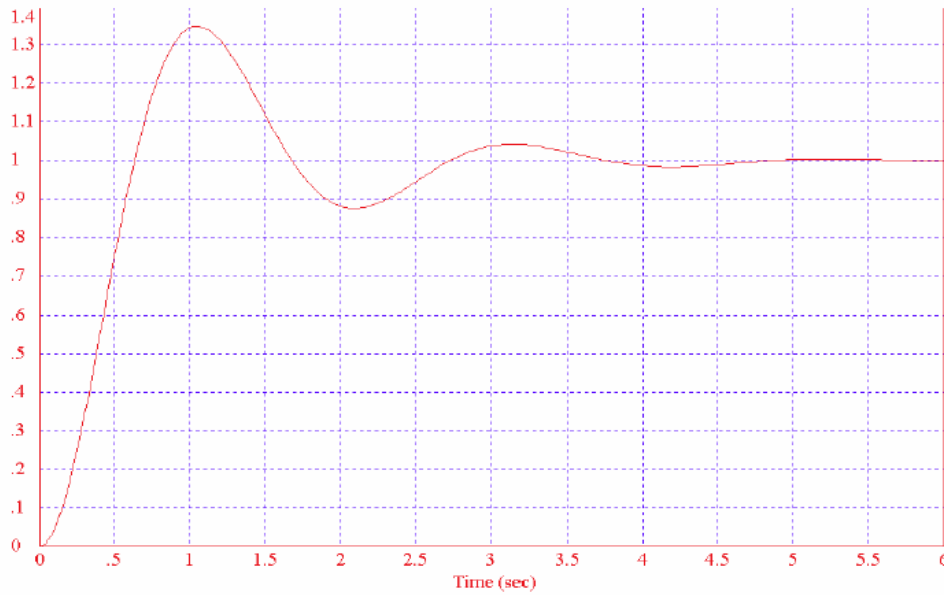


Find the transfer functions  $W_1(s) = V_c(s) / V_0(s)$

3. Using block-diagram transformations reduce given block-diagram. Identify the transfer function  $W(s) = Y(s) / R(s)$ . (6 pts)

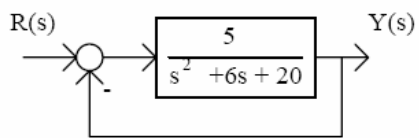


4. Given response of a prototype second order system to a unit-step function (fig.2). Identify a transfer function of this system.



5. For given system

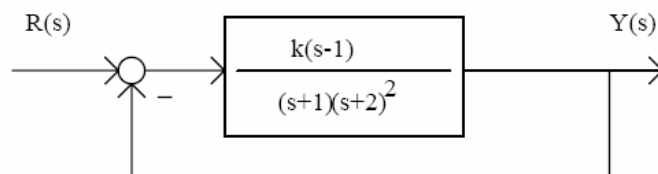
(6 pnts)



sketch the unit step response without mathematically solving for the time response, if  $r(t) = 1(t)$

6. Given the block-diagram

(6 points)



Use Routh criterion of stability to calculate the range  $a < k < b$  that makes the closed loop system stable if any.

1. Carefully sketch a root locus for a close-loop control system:



where  $G(s) = \frac{K}{(s+4)^2(s+1)}$ . Find the value of  $K$  for which the close-loop system is marginally stable, if any.